## $38^{\text {th }}$



# International Chemistry Olympiad 

11 theoretical problems
3 practical problems

# THE THIRTY-EIGHTH <br> INTERNATIONAL CHEMISTRY OLYMPIAD 2-11 JULY 2006, GYEONGSAN, KOREA 

## THEORETICAL PROBLEMS

## PROBLEM 1

## Avogadro's number

Spherical water droplets are dispersed in argon gas. At $27^{\circ} \mathrm{C}$, each droplet is 1.0 micrometer in diameter and undergoes collisions with argon. Assume that inter-droplet collisions do not occur. The root-mean-square speed of these droplets was determined to be $0.50 \mathrm{~cm} \mathrm{~s}^{-1}$ at $27^{\circ} \mathrm{C}$. The density of a water droplet is $1.0 \mathrm{~g} \mathrm{~cm}^{-3}$.

### 1.1 Calculate the average kinetic energy $\left(\mathrm{mv}^{2} / 2\right)$ of this droplet at $27^{\circ} \mathrm{C}$. The volume of a

 sphere is given by $(4 / 3) \pi r^{3}$ where $r$ is the radius.If the temperature is changed, then droplet size and speed of the droplet will also change. The average kinetic energy of a droplet between $0^{\circ} \mathrm{C}$ and $100{ }^{\circ} \mathrm{C}$ as a function of temperature is found to be linear. Assume that it remains linear below $0^{\circ} \mathrm{C}$.


At thermal equlibrium, the average kinetic energy is the same irrespective of particle masses (equipartition theorem).

The specific heat capacity, at constant volume, of argon (atomic weight, 40) gas is $0.31 \mathrm{~J} \mathrm{~g}^{-1} \mathrm{~K}^{-1}$.
1.2. Calculate Avogadro's number without using the ideal gas law, the gas constant, Boltzmann's constant).

## SOLUTION

1.1 The mass of a water droplet:

$$
m=V \rho=\left[(4 / 3) \pi r^{3}\right] \rho=(4 / 3) \pi\left(0.5 \times 10^{-6} \mathrm{~m}\right)^{3}\left(1.0 \mathrm{~g} \mathrm{~cm}^{-3}\right)=5.2 \times 10^{-16} \mathrm{~kg}
$$

Average kinetic energy at $27^{\circ} \mathrm{C}$ :

$$
E_{k}=\frac{m v^{2}}{2}=\frac{\left(5.2 \times 10^{-16} \mathrm{~kg}\right) \times\left(0.51 \times 10^{-2} \mathrm{~m} / \mathrm{s}\right)^{2}}{2}=6.9 \times 10^{-21} \mathrm{~kg} \mathrm{~m}^{2} / \mathrm{s}^{2}=\underline{6.9 \times 10^{-21} \mathrm{~J}}
$$

1.2 The average kinetic energy of an argon atom is the same as that of a water droplet. $E_{k}$ becomes zero at $-273^{\circ} \mathrm{C}$.

From the linear relationship in the figure, $E_{k}=a T$ (absolute temperature) where $a$ is the increase in kinetic energy of an argon atom per degree.
$\mathrm{a}=\frac{E_{k}}{T}=\frac{6.9 \times 10^{-21} \mathrm{~J}}{(27+273) \mathrm{K}}=2.3 \times 10^{-23} \mathrm{~J} \mathrm{~K}^{-1}$
$S$ : specific heat of argon $\quad N$ : number of atoms in 1 g of argon
$S=0.31 \mathrm{Jg}^{-1} \mathrm{~K}^{-1}=a \times N$
$N=\frac{S}{a}=\frac{0.31 \mathrm{~J} \mathrm{~g}^{-1} \mathrm{~K}^{-1}}{2.3 \times 10^{-23} \mathrm{JK}^{-1}}=1.4 \times 10^{22} \mathrm{~g}^{-1}$
Avogadro's number $\left(N_{A}\right)$ : Number of argon atoms in 40 g of argon
$N_{A}=40 \mathrm{~g} \mathrm{~mol}^{-1} \times 1.4 \times 10^{22} \mathrm{~g}^{-1}=\underline{5.6 \times 10^{23} \mathrm{~mol}^{-1}}$

## PROBLEM 2

## Detection of hydrogen

Hydrogen is prevalent in the universe. Life in the universe is ultimately based on hydrogen.
2.1 There are about $1 \times 10^{23}$ stars in the universe. Assume that they are like our sun (radius, $700,000 \mathrm{~km}$; density, $1.4 \mathrm{~g} \mathrm{~cm}^{-3} ; 3 / 4$ hydrogen and $1 / 4$ helium by mass). Estimate the number of stellar protons in the universe to one significant figure.

In the 1920s Cecilia Payne discovered by spectral analysis of starlight that hydrogen is the most abundant element in most stars.
2.2 The electronic transition of a hydrogen atom is governed by $\Delta E\left(n_{i} \rightarrow n_{f}\right)=$ $=-C\left(1 / n_{f}^{2}-1 / n_{i}^{2}\right)$, where $n$ is principle quantum number, and $C$ is a constant. For detection of the $\Delta E(3 \rightarrow 2)$ transition ( 656.3 nm in the Balmer series), the electron in the ground state of the hydrogen atom needs to be excited first to the $n=2$ state. Calculate the wavelength (in nm ) of the absorption line in the starlight corresponding to the $\Delta E(1 \rightarrow 2)$ transition.
2.3 According to Wien's law, the wavelength $(\lambda)$ corresponding to the maximum light intensity emitted from a blackbody at temperature $T$ is given by $\lambda T=2.9 \times 10^{-3} \mathrm{~m} \mathrm{~K}$. Calculate the surface temperature of a star whose blackbody radiation has a peak intensity corresponding to the $n=1 \rightarrow n=2$ excitation of hydrogen.

The ground state of hydrogen is split into two hyperfine levels due to the interaction between the magnetic moment of the proton and that of the electron. In 1951, Purcell discovered a spectral line at 1420 MHz due to the hyperfine transition of hydrogen in interstellar space.
2.4 Hydrogen in interstellar space cannot be excited electronically by starlight. However, the cosmic background radiation, equivalent to 2.7 K , can cause the hyperfine transition. Calculate the temperature of a blackbody whose peak intensity corresponds to the 1420 MHz transition.
2.5 Wien generated hydrogen ions by discharge of hydrogen gas at a very low pressure and determined the e/m value, which turned out to be the highest among different
gases tested. In 1919, Rutherford bombarded nitrogen with alpha-particles and observed emission of a positively charged particle which turned out to be the hydrogen ion observed by Wien. Rutherford named this particle the "proton". Fill in the blank.

## SOLUTION

2.1 Mass of a typical star $=(4 / 3) \times(3.1) \times\left(7 \times 10^{8} \mathrm{~m}\right)^{3} \times\left(1.4 \times 10^{6} \mathrm{~g} \mathrm{~m}^{-3}\right)=2 \times 10^{33} \mathrm{~g}$

Mass of protons of a typical star $=\left(2 \times 10^{33} \mathrm{~g}\right) \times(3 / 4+1 / 8)=1.8 \times 10^{33} \mathrm{~g}$
Number of protons of a typical star $=\left(1.8 \times 10^{33} \mathrm{~g}\right) \times\left(6 \times 10^{23} \mathrm{~g}^{-1}\right)=1 \times 10^{57}$
Number of stellar protons in the universe $=\left(1 \times 10^{57}\right) \times\left(10^{23}\right)=\underline{1 \times 10^{80}}$
$2.2 \Delta E(2 \rightarrow 3)=C(1 / 4-1 / 9)=0.1389 C \quad \lambda(2 \rightarrow 3)=656.3 \mathrm{~nm}$
$\Delta E(1 \rightarrow 2)=C(1 / 1-1 / 4)=0.75 C$
$\lambda(1 \rightarrow 2)=(656.3) \times(0.1389 / 0.75)=121.5 \mathrm{~nm}$
$2.3 T=2.9 \times 10^{-3} \mathrm{~m} \mathrm{~K} / 1.215 \times 10^{-7} \mathrm{~m}=2.4 \times 10^{4} \mathrm{~K}$
$2.4 \lambda=3 \times 10^{8} \mathrm{~m} / 1.42 \times 10^{9}=0.21 \mathrm{~m}$

$$
T=2.9 \times 10^{-3} \mathrm{~m} \mathrm{~K} / 0.21 \mathrm{~m}=0.014 \mathrm{~K}
$$

$2.5{ }^{14} \mathrm{~N}+{ }^{4} \mathrm{He} \rightarrow{ }^{17} \mathrm{O}+{ }^{1} \mathrm{H}$

## PROBLEM 3

## Interstellar chemistry

Early interstellar chemistry is thought to have been a prelude to life on Earth. Molecules can be formed in space via heterogeneous reactions at the surface of dust particles, often called the interstellar ice grains (IIGs). Imagine the reaction between H and C atoms on the IIG surface that forms CH . The CH product can either be desorbed from the surface or further react through surface migration with adsorbed H atoms to form $\mathrm{CH}_{2}$, $\mathrm{CH}_{3}$, etc.

Depending on how energetically a molecule "jumps" from its anchored site, it either leaves the surface permanently (desorption) or returns to a new position at the surface (migration). The rates of desorption and migratory jump follow the Arrhenius formula, $k=A \exp (-E / R T)$, where $k$ is the rate constant for desorption or migratory jump, $A$ the jumping frequency, and $E$ the activation energy for the respective event.
3.1 Desorption of CH from the IIG surface follows first-order kinetics. Calculate the average residence time of CH on the surface at 20 K . Assume that $A=1 \times 10^{12} \mathrm{~s}^{-1}$ and $E_{\text {des }}=12 \mathrm{~kJ} \mathrm{~mol}^{-1}$.
3.2 Consider the shortest time it would take for one CH unit to move from its initial position to the opposite side of an IIG by successive migratory jumps. Assume that the activation energy for migration $\left(E_{\text {mig }}\right)$ is $6 \mathrm{~kJ} \mathrm{~mol}^{-1}$, and the IIG is a sphere with a $0.1 \mu \mathrm{~m}$ radius. Each migratory jump laterally advances the molecule by 0.3 nm . Show work and choose your answer from (a) - (e) below.
(a) $t \leq 1$ day
(b) 10 days $\leq t \leq 10^{2} \mathrm{yr}$
C) $10^{3} \mathrm{yr} \leq t \leq 10^{6} \mathrm{yr}$
(d) $10^{7} \mathrm{yr} \leq t \leq 10^{10} \mathrm{yr}$
(e) $t \geq 10^{11} \mathrm{yr}$
3.3 Consider the reaction of CO with $\mathrm{H}_{2}$ to form $\mathrm{H}_{2} \mathrm{CO}$. The activation energy on a metal catalyst is $20 \mathrm{~kJ} \mathrm{~mol}^{-1}$ that is produced by formaldehyde at a rate of 1 molecule/s per site at 300 K . Estimate the rate of formaldehyde formation per site if the reaction takes place at 20 K .
3.4 Which is a set of all true statements? Circle one.
(a) Most CH species are desorbed from the IIG surface before encountering other reactants by surface migration.
(b) IIGs can assist transformation of simple molecules to more complex ones in interstellar space.
(c) For a reaction on the IIG to occur at an appreciable speed during the age of the Universe ( $1 \times 10^{10} \mathrm{yr}$ ), the reaction energy barrier must be absent or negligible.
$\square(a)$
(b)
(c)
$\square(a, b)$
$\square(a, c)$
$\square(b, c)$
$\square(a, b, c)$

## SOLUTION

$3.1 \quad k_{\text {des }}=A \exp \left(-E_{\text {des }} / R T\right)=\left(1 \times 10^{12} \mathrm{~s}^{-1}\right) \times\left(5 \times 10^{-32}\right)=5 \times 10^{-20} \mathrm{~s}^{-1}$ at $T=20 \mathrm{~K}$
surface residence time, $T_{\text {residence }}=1 / k_{\text {des }}=2 \times 10^{19} \mathrm{~s}=\underline{6} \times \underline{10^{11} \mathrm{yr}}$
(full credit for $T_{\text {half-life }}=\ln 2 / k_{\text {des }}=1 \times 10^{19} \mathrm{~s}=4 \times 10^{11} \mathrm{yr}$ )
residence time $=2 \times 10^{19} \mathrm{~s}$
3.2 The distance to be traveled by a molecule: $x=\pi r=300 \mathrm{~nm}$.
$k_{\text {mig }}=A \exp \left(-E_{\text {mig }} / R T\right)=\left(1 \times 10^{12} \mathrm{~s}^{-1}\right) \times\left(2 \times 10^{-16}\right)=2 \times 10^{-4} \mathrm{~s}^{-1}$ at $T=20 \mathrm{~K}$

Average time between migratory jumps, $T=1 / k_{\text {mig }}=5 \times 10^{3} \mathrm{~s}$
Time needed to move $300 \mathrm{~nm}=(300 \mathrm{~nm} / 0.3 \mathrm{~nm})$ jumps $\times\left(5 \times 10^{3} \mathrm{~s} / \mathrm{jump}\right)=$
$=5 \times 10^{6} \mathrm{~s}=\underline{50 \text { days }}$
The correct answer is (b).
(Full credit for the calculation using a random-walk model. In this case:
$t=T(x / d)^{2}=5 \times 10^{9} \mathrm{~s}=160 \mathrm{yr}$. The answer is still (b).)
$3.3 k(20 \mathrm{~K}) / k(300 \mathrm{~K})=\exp \left[(E / R)\left(1 / T_{1}-1 / T_{2}\right)\right]=\mathrm{e}^{-112}=\sim 1 \times 10^{-49}$ for the given reaction The rate of formaldehyde production at $20 \mathrm{~K}==\sim 1 \times 10^{-49}$ molecule/site/s $=$ $=\sim 1 \times 10^{-42}$ molecule/site/ yr
(The reaction will not occur at all during the age of the universe ( $1 \times 10^{10} \mathrm{yr}$ ).)
3.4 The correct answer is $(b, c)$.

## PROBLEM 4

## The Chemistry of DNA

4.1 In 1944 Oswald Avery isolated a genetic material and showed by elemental analysis that it was a sodium salt of deoxyribonucleic acid. A segment of DNA with formula mass of 1323.72 is shown.


Assuming that equimolar amounts of the four bases are present in DNA, write the number of H atoms per P atom. Calculate (to 3 significant figures) the theoretical weight percentage of H expected upon elemental analysis of DNA.
4.2 Chargaff extracted the separated bases and determined their concentrations by measuring UV absorbance. The Beer-Lambert law was used to obtain the molar concentration. Chargaff discovered the following molar ratio for bases in DNA:

$$
\begin{aligned}
& \text { adenine to guanine }=1.43 \quad \text { thymine to cytosine }=1.43 \\
& \text { adenine to thymine }=1.02 \quad \text { guanine to cytosine }=1.02
\end{aligned}
$$

Chargaff's discovery suggested that the bases might exist as pairs in DNA. Watson and Crick mentioned in their celebrated 1953 paper in Nature: "It has not escaped our notice that the specific pairing we have postulated immediately suggests a possible copying mechanism for the genetic material."

Draw structures of the specific pairing found in DNA. Indicate hydrogen bonds. Omit the sugar-phosphate backbone.
4.3 Mutation can occur through base pairings different from the above. Draw structures of any three alternative base pairs.
4.4 The plausibility of the formation of purine and pyrimidine bases in the prebiotic atmosphere of the Earth from $\mathrm{HCN}, \mathrm{NH}_{3}$, and $\mathrm{H}_{2} \mathrm{O}$ has been demonstrated in the laboratory. Write the minimum number of HCN and $\mathrm{H}_{2} \mathrm{O}$ molecules required for formation of the following compounds.

adenine

guanine


Uracil

cytosine

## SOLUTION

## 4.1

H P
Number of atoms: 11.31
theoretical wt \%:
3.43

## 4.2



adenine
thymine

## 4.3


cytosine

adenine

cytosine cytosine

thymine thymine


adenine


guanine
guanine

adenine
adenine

## 4.4



## PROBLEM 5

## Acid-Base Chemistry

5.1 Calculate $\left[\mathrm{H}^{+}\right],\left[\mathrm{OH}^{-}\right],\left[\mathrm{HSO}_{4}{ }^{-}\right]$, and $\left[\mathrm{SO}_{4}{ }^{2-}\right]$ in a $1.0 \times 10^{-7} \mathrm{M}$ solution of sulfuric acid ( $K_{w}=1.0 \times 10^{-14}, K_{2}=1.2 \times 10^{-2}$ at $25{ }^{\circ} \mathrm{C}$ ). In your work you may use mass- and charge-balance equations. Answer with two significant figures.
5.2 Calculate the volume of 0.80 M NaOH solution that should be added to a $250 \mathrm{~cm}^{3}$ aqueous solution containing $3.48 \mathrm{~cm}^{3}$ of concentrated phosphoric acid in order to prepare a pH 7.4 buffer. Answer with three significant figures. $\left(\mathrm{H}_{3} \mathrm{PO}_{4}(\mathrm{aq})\right.$, purity $=$ 85 mass $\%$, density $\left.=1.69 \mathrm{~g} / \mathrm{cm}^{3}, M_{r}=98.00\right)\left(\mathrm{p} K_{1}=2.15, \mathrm{p} K_{2}=7.20, \mathrm{p} K_{3}=12.44\right)$.
5.3 The efficacy of a drug is greatly dependent on its ability to be absorbed into the blood stream. Acid-base chemistry plays an important role in drug absorption.


Assume that the ionic form ( $A^{-}$) of a weakly acidic drug does not penetrate the membrane, whereas the neutral form (HA) freely crosses the membrane. Also assume that equilibrium is established so that the concentration of HA is the same on both sides. Calculate the ratio of the total concentration ([HA] + [A]) of aspirin (acetylsalicylic acid, $\mathrm{p} K=3.52$ ) in the blood to that in the stomach.

## SOLUTION

5.1 1st ionization is complete: $\mathrm{H}_{2} \mathrm{SO}_{4} \rightarrow \mathrm{H}^{+}+\mathrm{HSO}_{4}^{-}$
$\left[\mathrm{H}_{2} \mathrm{SO}_{4}\right]=0$

2nd ionization: $\left[\mathrm{H}^{+}\right]\left[\mathrm{SO}_{4}^{2-}\right] /\left[\mathrm{HSO}_{4}^{-}\right]=K_{2}=1.2 \times 10^{-2}$
Mass balance: $\left[\mathrm{H}_{2} \mathrm{SO}_{4}\right]+\left[\mathrm{HSO}_{4}^{-}\right]+\left[\mathrm{SO}_{4}^{2-}\right]=1.0 \times 10^{-7}$
Charge balance: $\left[\mathrm{H}^{+}\right]=\left[\mathrm{HSO}_{4}^{-}\right]+2\left[\mathrm{SO}_{4}^{2-}\right]+\left[\mathrm{OH}^{-}\right]$
Degree of ionization is increased upon dilution.
$\left[\mathrm{H}_{2} \mathrm{SO}_{4}\right]=0$
Assume $\left[\mathrm{H}^{+}\right]_{\mathrm{H}_{2} \mathrm{SO}_{4}}=2 \times 10^{-7}$
From (1): $\left[\mathrm{SO}_{4}^{2-}\right] /\left[\mathrm{HSO}_{4}^{-}\right]=6 \times 10^{4}$ (2nd ionization is almost complete)
$\left[\mathrm{HSO}_{4}^{-}\right]=0$
From (2): $\left[\mathrm{SO}_{4}^{2-}\right]=1.0 \times 10^{-7}$
From (3): $\left[\mathrm{H}^{+}\right]=\left(2 \times 10^{-7}\right)+10^{-14} /\left[\mathrm{H}^{+}\right]$
$\left[\mathrm{H}^{+}\right]=2.4 \times 10^{-7} \quad(\mathrm{pH}=6.6)$
$\left[\mathrm{OH}^{-}\right]=1 \times 10^{-14} /\left(2.4 \times 10^{-7}\right)=4.1 \times 10^{-8}$

From (1):
$\left[\mathrm{HSO}_{4}^{-}\right]=\left[\mathrm{H}^{+}\right]\left[\mathrm{SO}_{4}^{2-}\right] / K_{2}=\left(2.4 \times 10^{-7}\right) \times\left(1.0 \times 10^{-7}\right) /\left(1.2 \times 10^{-2}\right)=2.0 \times 10^{-12}$

Check charge balance:
$2.4 \times 10^{-7} \approx\left(2.0 \times 10^{-12}\right)+2\left(1.0 \times 10^{-7}\right)+\left(4.1 \times 10^{-8}\right)$
Check mass balance:

$$
0+2.0 \times 10^{-12}+1.0 \times 10^{-7} \approx 1.0 \times 10^{-7}
$$

$5.2 n\left(\mathrm{H}_{3} \mathrm{PO}_{4}\right)=0.85 \times 3.48 \mathrm{~cm}^{3} \times 1.69 \mathrm{~g} \mathrm{~cm}^{-3} \times 1 \mathrm{~mol} / 98.00 \mathrm{~g} \times 1000=51.0 \mathrm{mmol}$ The desired pH is above $\mathrm{p} K_{2}$.

A $1: 1$ mixture of $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$and $\mathrm{HPO}_{4}^{2-}$ would have $p H=p K_{2}=7.20$.
If the pH is to be 7.40 , there must be more $\mathrm{HPO}_{4}^{2-}$ than $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$.
We need to add NaOH to convert $\mathrm{H}_{3} \mathrm{PO}_{4}$ to $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$and to convert to the right amount of $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$to $\mathrm{HPO}_{4}^{2-}$.

$$
\begin{aligned}
& \mathrm{H}_{3} \mathrm{PO}_{4}+\mathrm{OH}^{-} \rightarrow \mathrm{H}_{2} \mathrm{PO}_{4}^{-}+\mathrm{H}_{2} \mathrm{O} \\
& \mathrm{H}_{2} \mathrm{PO}_{4}^{-}+\mathrm{OH}^{-} \rightarrow \mathrm{HPO}_{4}^{2-}+\mathrm{H}_{2} \mathrm{O}
\end{aligned}
$$

The volume of 0.80 NaOH needed to react with to convert $\mathrm{H}_{3} \mathrm{PO}_{4}$ to $\mathrm{H}_{2} \mathrm{PO}_{4}^{-}$is:
$51.0 \mathrm{mmol} / 0.80 \mathrm{~mol} \mathrm{dm}^{-3}=63.75 \mathrm{~cm}^{3}$

To get pH of 7.40 we need:

$$
\mathrm{H}_{2} \mathrm{PO}_{4}^{-}+\mathrm{OH}^{-} \rightarrow \mathrm{HPO}_{4}^{2-}
$$

| Initial mmol | 51.0 | $x$ | 0 |
| :--- | :---: | :---: | :---: |
| Final mmol | $51.0-\mathrm{x}$ | 0 | x |

$p H=p K_{2}+\log \left[\mathrm{HPO}_{4}^{2-}\right] /\left[\mathrm{H}_{2} \mathrm{PO}_{4}^{-}\right]$
$7.40=7.20+\log \{x /(51.0-x)\} ; \quad x=31.27 \mathrm{mmol}$
The volume of NaOH needed to convert 31.27 mmol is:
$31.27 \mathrm{mmol} / 0.80 \mathrm{~mol} \mathrm{dm}^{-3}=39.09 \mathrm{~cm}^{3}$
The total volume of $\mathrm{NaOH}=63.75+39.09=102.84 \mathrm{~cm}^{3} \approx 103 \mathrm{~cm}^{3}$
$5.3 \mathrm{pK}=3.52$
$p H=p K_{a}+\log ([A] /[H A])$
$\left[\mathrm{A}^{-}\right] /[\mathrm{HA}]=10^{(\mathrm{pH}-\mathrm{pKa})}$

In blood, $\mathrm{pH}=7.40, \quad[\mathrm{~A}] /[\mathrm{HA}]=10^{(7.40-3.52)}=7586$
Total ASA $=7586+1=7587$

In stomach, $\mathrm{pH}=2.00,[\mathrm{~A}] /[\mathrm{HA}]=10^{(2.00-3.52)}=3.02 \times 10^{-2}$
Total ASA $=1+3.02 \times 10^{-2}=1.03$
Ratio of total aspirin in blood to that in stomach $=7587 / 1.03=7400$

## PROBLEM 6

## Electrochemistry

Water is a very stable molecule, abundant on earth and essential for life. As such, water was long thought to be a chemical element. However, soon after the invention of a voltaic cell in 1800, Nicholson and Carlyle decomposed water into hydrogen and oxygen by electrolysis.
6.1 Water can be thought of as hydrogen oxidized by oxygen. Thus, hydrogen can be recovered by reduction of water, using an aqueous solution of sodium sulfate, at a platinum electrode connected to the negative terminal of a battery. The solution near the electrode becomes basic. Write a balanced half-reaction for the reduction of water.
6.2 Water can also be thought of as oxygen reduced by hydrogen. Thus, oxygen can be recovered by oxidation of water at the Pt electrode connected to the positive terminal. Write a balanced half-reaction for the oxidation of water.
6.3 When copper is used at both electrodes, gas is generated only at one electrode during the initial stage of electrolysis. Write the half-reaction at the electrode that does not generate gas.

Another species in solution that can be reduced is sodium ion. The reduction of sodium ion to metallic sodium does not occur in aqueous solution because water is reduced first. However, as Humphrey Davy discovered in 1807, sodium can be made by electrolysis of fused sodium chloride.
6.4 Based on these observations, connect the half-reactions with the standard reduction potential (in volts).
Reduction of copper ion $\left(\mathrm{Cu}^{2+}\right) \quad+0.340$
Reduction of oxygen - 2.710
Reduction of water -0.830
Reduction of sodium ion $\left(\mathrm{Na}^{+}\right) \quad 0.000$
Reduction of hydrogen ion +1.230

The electrode potential is affected by other reactions taking place around the electrode. The potential of the $\mathrm{Cu}^{2+} / \mathrm{Cu}$ electrode in a $0.100 \mathrm{M} \mathrm{Cu}^{2+}$ solution changes as $\mathrm{Cu}(\mathrm{OH})_{2}$ precipitates. Answer with 3 significant figures for the following problems. The temperature is $25{ }^{\circ} \mathrm{C}$. Note that $K_{w}=1.00 \times 10^{-14}$ at $25^{\circ} \mathrm{C}$.
6.5 Precipitation of $\mathrm{Cu}(\mathrm{OH})_{2}$ begins at $\mathrm{pH}=4.84$. Determine the solubility product of $\mathrm{Cu}(\mathrm{OH})_{2}$.
6.6 Calculate the standard reduction potential for $\mathrm{Cu}(\mathrm{OH})_{2}(\mathrm{~s})+2 \mathrm{e}^{-} \rightarrow \mathrm{Cu}(\mathrm{s})+2 \mathrm{OH}^{-}$.
6.7 Calculate the electrode potential at $\mathrm{pH}=1.00$.

Lithium cobalt oxide and specialty carbon are active ingredients for the positive and negative electrodes, respectively, of a rechargeable lithium battery. During the charge recharge cycles, the following reversible half-reactions occur.
$\mathrm{LiCoO}_{2} \rightleftarrows \mathrm{Li}_{1-\mathrm{x}} \mathrm{CoO}_{2}+\mathrm{xil}^{+}+\mathrm{xe}^{-}$
$\mathrm{C}+\mathrm{xLi}{ }^{+}+\mathrm{xe} \mathrm{e}^{-} \rightleftarrows \mathrm{CLi}_{\mathrm{x}}$
The total amount of energy a battery can store, is rated in mAh. A battery rated at 1500 mAh can power a device drawing 100 milliamps for 15 hours.
6.8 Graphite has lithium intercalation sites between its layers. Assuming a maximum $6: 1$ carbon-to-lithium intercalation stoichiometry, calculate the theoretical charge capacity of 1.00 gram of graphite to intercalate lithium. Answer in mAh/g with 3 significant figures.

## SOLUTION

6.1 $4 \mathrm{H}_{2} \mathrm{O}+4 \mathrm{e}^{-} \rightarrow 2 \mathrm{H}_{2}(\mathrm{~g})+4 \mathrm{OH}^{-}\left(\right.$or $\left.2 \mathrm{H}_{2} \mathrm{O}+2 \mathrm{e}^{-} \rightarrow \mathrm{H}_{2}(\mathrm{~g})+2 \mathrm{OH}^{-}\right)$
$6.22 \mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{O}_{2}+4 \mathrm{H}^{+}+4 \mathrm{e}^{-} \quad\left(\right.$ or $\left.\mathrm{H}_{2} \mathrm{O} \rightarrow 1 / 2 \mathrm{O}_{2}+2 \mathrm{H}^{+}+2 \mathrm{e}^{-}\right)$
6.3 $\mathrm{Cu} \rightarrow \mathrm{Cu}^{2+}+2 \mathrm{e}^{-}$
6.4 Reduction of sodium ion seldom takes place.

It has a highly negative reduction potential of -2.710 V .

Reduction potential for water to hydrogen is negative (water is very stable).
But, it is not as negative as that for sodium ion. It is -0.830 V .
Reduction of both copper ion and oxygen takes place readily and the reduction potentials for both are positive.
In the present system, the reverse reaction (oxidation) takes place at the positive terminal. Copper is oxidized before water.

Reduction potential for hydrogen ion is defined as 0.000 V .

| Reduction of oxygen | -2.710 |
| :---: | :---: |
| Reduction of water | -0.830 |
| Reduction of sodium ion $\left(\mathrm{Na}^{+}\right)$ | 0.000 |
| Reduction of hydrogen ion | +1.230 |

$6.5 \mathrm{pOH}=14.00-4.84=9.16$
$\left[\mathrm{OH}^{-}\right]=6.92 \times 10^{-10}$
$K_{s p}=\left[\mathrm{Cu}^{2+}\right]\left[\mathrm{OH}^{-}\right]^{2}=0.100 \times\left(6.92 \times 10^{-10}\right)=4.79 \times 10^{-20}$
6.6 $E=E^{\circ}\left(\mathrm{Cu}^{2+} / \mathrm{Cu}\right)+(0.0592 / 2) \log \left[\mathrm{Cu}^{2+}\right]=+0.340+(0.0592 / 2) \log \left[\mathrm{Cu}^{2+}\right]=$

$$
=+0.340+(0.0592 / 2) \log \left(K_{\text {sp }} /\left[\mathrm{OH}^{-}\right]^{2}\right)
$$

$$
\begin{aligned}
& =+0.340+(0.0592 / 2) \log K_{s p}-(0.0592 / 2) \log \left[\mathrm{OH}^{-}\right]^{2} \\
& =+0.340+(0.0592 / 2) \log K_{s p}-0.0592 \log \left[\mathrm{OH}^{-}\right]
\end{aligned}
$$

By definition, the standard potential for

$$
\mathrm{Cu}(\mathrm{OH})_{2}(\mathrm{~s})+2 \mathrm{e}^{-} \rightarrow \mathrm{Cu}(\mathrm{~s})+2 \mathrm{OH}^{-}
$$

is the potential where $\left[\mathrm{OH}^{-}\right]=1.00$.

$$
\begin{aligned}
E & =E^{o}\left(\mathrm{Cu}(\mathrm{OH})_{2} / \mathrm{Cu}\right)=+0.340+(0.0592 / 2) \log K_{s p} \\
& =+0.340+(0.0592 / 2) \log \left(4.79 \times 10^{-20}\right) \\
& =+0.340-0.572 \\
& =-0.232 \mathrm{~V}
\end{aligned}
$$

One may solve this problem as follows.
Eqn 1: $\mathrm{Cu}(\mathrm{OH})_{2}(\mathrm{~s})+2 \mathrm{e}^{-} \rightarrow \mathrm{Cu}+2 \mathrm{OH}^{-}$
$E_{+}{ }^{\circ}=E^{\circ}\left(\mathrm{Cu}(\mathrm{OH})_{2} / \mathrm{Cu}\right)=$ ?

Eqn 2: $\mathrm{Cu}(\mathrm{OH})_{2}(\mathrm{~s}) \rightarrow \mathrm{Cu}^{2+}+2 \mathrm{OH}^{-}$
$E^{\circ}=(0.05916 / n) \log K_{s p}=(0.05916 / 2) \log \left(4.79 \times 10^{-20}\right)=-0.5715 \mathrm{~V}$

Eqn 1 - Eqn $2: \mathrm{Cu}^{2+}+2 \mathrm{e}^{-} \rightarrow \mathrm{Cu}$
$E_{-}^{0}=E_{+}{ }^{\circ}-E^{0}=E^{0}\left(\mathrm{Cu}^{2+} / \mathrm{Cu}\right)=0.34 \mathrm{~V}$
Therefore, $E_{+}{ }^{0}=E_{-}{ }^{0}+E^{0}=+0.34+(-0.5715)==-0.232 \mathrm{~V}$
6.7 Below $\mathrm{pH}=4.84$, there is no effect of $\mathrm{Cu}(\mathrm{OH})_{2}$ because of no precipitation.

Therefore,

$$
\begin{aligned}
E=E\left(\mathrm{Cu}^{2+} / \mathrm{Cu}\right) & =+0.340+(0.0592 / 2) \log \left[\mathrm{Cu}^{2+}\right]= \\
= & +0.340+(0.0592 / 2) \log 0.100=+0.340-0.0296=+0.310 \mathrm{~V}
\end{aligned}
$$

6.81 .00 g graphite $=0.0833 \mathrm{~mol}$ carbon

6 mol carbon to 1 mol lithium; 1 g graphite can hold 0.0139 mol lithium
To insert 1 mol lithium, 96487 coulombs are needed.
Therefore, 1 g graphite can charge $96487 \times 0.0139=1340$ coulombs.
1340 coulombs $/ \mathrm{g}=1340 \mathrm{~A} \sec / \mathrm{g}=1340 \times 1000 \mathrm{~mA} \times(1 / 3600) \mathrm{h}=$
$=372 \mathrm{mAh} / \mathrm{g}$

## PROBLEM 7

## Hydrogen Economy

Hydrogen is more energy-dense than carbon, by mass. Thus, historically there has been a move toward fuel with higher hydrogen content: coal $\rightarrow$ oil $\rightarrow$ natural gas $\rightarrow$ hydrogen. Cost-effective production and safe storage of hydrogen are two major hurdles to the successful inauguration of a hydrogen economy.
7.1 Consider hydrogen in a cylinder of 80 MPa at $25^{\circ} \mathrm{C}$. Using the ideal gas law, estimate the density of hydrogen in the cylinder in $\mathrm{kg} \mathrm{m}^{-3}$.
7.2 Calculate the ratio between heat generated when hydrogen is burned and heat generated when the same weight of carbon is burned. The difference comes to a large extent from the fact that the most abundant isotope of hydrogen has no neutron and hydrogen has no inner electron shell. $\Delta H_{f}^{0}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{I})\right]=-286 \mathrm{~kJ} / \mathrm{mol}, \Delta H_{\mathrm{f}}^{0}$ $\left[\mathrm{CO}_{2}(\mathrm{~g})\right]=-394 \mathrm{~kJ} / \mathrm{mol}$.
7.3 Calculate the theoretical maximum work produced by the combustion of 1 kg hydrogen (a) from the electric motor using hydrogen fuel cell and (b) from the heat engine working between $25{ }^{\circ} \mathrm{C}$ and $300{ }^{\circ} \mathrm{C}$. The efficiency (work done/heat absorbed) of an ideal heat engine working between $T_{\text {cold }}$ and $T_{\text {hot }}$ is given by [ $1-T_{\text {cold }} / T_{\text {hot }}$.
$\mathrm{S}^{\circ}{ }_{298}\left[\mathrm{H}_{2}(\mathrm{~g})\right]=131 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$
$S^{\circ}{ }_{298}\left[\mathrm{O}_{2}(\mathrm{~g})\right]=205 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$
$\mathrm{S}^{\circ}{ }_{298}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{I})\right]=70 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$

If the fuel cell is working at 1 W and the standard potential difference, how long will the electric motor run at what current?

## SOLUTION

$7.1 \frac{n}{V}=\frac{p}{R T}=\frac{80 \times 10^{6} \mathrm{~Pa}}{8,314 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1} \times 298 \mathrm{~K}}=32 \mathrm{kmol} \mathrm{m}^{-3}$
$\rho=\frac{m}{V}=32 \mathrm{kmol} \mathrm{m}^{-3} \times 2 \mathrm{~kg} \mathrm{kmol}^{-1}=64 \mathrm{~kg} \mathrm{~m}^{-3}$

7-2. $\mathrm{Hg}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{I}) ; \quad \Delta H_{\text {rexn-1 }}=\Delta H_{f}\left[\mathrm{H}_{2} \mathrm{O}(\mathrm{I})\right]=-286 \mathrm{~kJ} \mathrm{~mol}^{-1}=-143 \mathrm{~kJ} \mathrm{~g}^{-1}$
$\mathrm{C}(\mathrm{s})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g}) ; \quad \Delta H_{\text {rexn-2 }}=\Delta H_{f}\left[\mathrm{CO}_{2}(\mathrm{~g})\right]=-394 \mathrm{~kJ} \mathrm{~mol}^{-1}=-33 \mathrm{~kJ} \mathrm{~g}^{-1}$ $\frac{\left(-\Delta H_{\text {rexn-1 }}\right)}{\left(-\Delta H_{\text {rexn-2 }}\right)}=4.3$ or $\frac{\left(-\Delta H_{\text {rexn-2 }}\right)}{\left(-\Delta H_{\text {rexn-1 }}\right)}=0.23$
$7.3 \quad \mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{I})$
$\Delta H_{c}=-286 \mathrm{~kJ} \mathrm{~mol}^{-1}=-143 \mathrm{~kJ} \mathrm{~g}^{-1}=-143 \times 10^{3} \mathrm{~kJ} \mathrm{~kg}^{-1}$
$\Delta G=\Delta H-T \Delta S$
$\Delta S_{c}=70-131-205 / 2=-163.5 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$
$\Delta G_{c}=-286 \mathrm{~kJ} \mathrm{~mol}^{-1}+298 \mathrm{~K} \times 163.5 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}=-237 \mathrm{~kJ} \mathrm{~mol}^{-1}=-1.2 \times 10^{5} \mathrm{~kJ} \mathrm{~kg}^{-1}$
(a) electric motor: $\quad W_{\max }=\Delta G_{c} \times 1 \mathrm{~kg}=-1.2 \times 10^{5} \mathrm{~kJ}$
(b) heat engine: $\quad W_{\max }=$ efficiency $\times \Delta H_{c}$

$$
=(1-298 / 573) \times\left(-143 \times 10^{3} \mathrm{~kJ}\right)=-6.9 \times 10^{4} \mathrm{~kJ}
$$

$119 \times 10^{3} \mathrm{~kJ}=1 \mathrm{~W} \times \mathrm{t}(\mathrm{sec})$
$t=1.2 \times 10^{8} \mathrm{~s}=3.3 \times 10^{4} \mathrm{~h}=1.4 \times 10^{3}$ days $=46$ month $=3.8 \mathrm{yr}$
$\Delta G=-n F E \quad n=$ number of electrons involved in the reaction $F=96.5 \mathrm{kC} \mathrm{mol}^{-1}$
$\mathrm{H}_{2}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{H}_{2} \mathrm{O}(\mathrm{I}) \quad \mathrm{n}=2$
$E=\frac{-\Delta G}{n F}=\frac{237 \mathrm{~kJ} \mathrm{~mol}^{-1}}{2 \times 96.5 \mathrm{kC} \mathrm{mol}^{-1}}=1.23 \mathrm{~V}$
$I=\frac{W}{E}=0.81 \mathrm{~A}$

## PROBLEM 8

## Chemistry of Iron Oxides

The nucleus of iron is the most stable among all elements and, therefore, iron accumulates at the core of massive red giant stars where nucleosynthesis of many elements essential for life (such as $\mathrm{C}, \mathrm{N}, \mathrm{O}, \mathrm{P}, \mathrm{S}$, etc.) takes place. As a result, among heavy elements iron is quite abundant in the universe. Iron is also abundant on Earth.

Development of a technology for reducing iron oxide to iron was a key step in human civilization. Key reactions taking place in the blast furnace are summarized below.

$$
\begin{array}{ll}
\mathrm{C}(\mathrm{~s})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g}) & \Delta H^{0}=-393.51 \mathrm{~kJ}(/ \mathrm{mol}) \\
\mathrm{CO}_{2}(\mathrm{~g})+\mathrm{C}(\mathrm{~s}) \rightarrow 2 \mathrm{CO}(\mathrm{~g}) & \Delta H^{0}=172.46 \mathrm{~kJ}(/ \mathrm{mol}) \\
\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})+\mathrm{CO}(\mathrm{~g}) \rightarrow \mathrm{Fe}(\mathrm{~s})+\mathrm{CO}_{2}(\mathrm{~g}) & \Delta H^{0}=?
\end{array}
$$

8.1 Indicate the reducing agent in each reaction.
8.2 Balance reaction (3) and calculate the equilibrium constant of reaction (3) at $1200{ }^{\circ} \mathrm{C} . \Delta H_{\mathrm{f}}^{\circ}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})=-824.2 \mathrm{~kJ} \mathrm{~mol}^{-1}\right.$,
$S^{9}\left(\mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}\right): \mathrm{Fe}(\mathrm{s})=27.28, \mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})=87.40, \mathrm{C}(\mathrm{s})=5.74, \mathrm{CO}(\mathrm{g})=197.674$, $\mathrm{CO}_{2}(\mathrm{~g})=213.74$

In the manufacture of celadon pottery, $\mathrm{Fe}_{2} \mathrm{O}_{3}$ is partially reduced in a charcoal kiln to mixed oxides of $\mathrm{Fe}_{3} \mathrm{O}_{4}$ and FeO . The amount of the different oxides seems to be related to the "mystic" color of celadon ceramics. $\mathrm{Fe}_{3} \mathrm{O}_{4}$ (magnetite) itself is
 a mixed oxide containing $\mathrm{Fe}^{2+}$ and $\mathrm{Fe}^{3+}$ ions and belongs to a group of compounds with a general formula of $\mathrm{AB}_{2} \mathrm{O}_{4}$. The oxide ions form a face-centered cubic array. The figure shows the array of oxygens (gray circles) and representative sites for divalent $A$ and trivalent $B$ cations. The dark circle represents a tetrahedral site and the white circle an octahedral site.

8.3 How many available octahedral sites for iron ions are there in one $\mathrm{AB}_{2} \mathrm{O}_{4}$ unit? Certain sites are shared by neighbouring units.
$\mathrm{AB}_{2} \mathrm{O}_{4}$ can adopt a normal- or an inverse-spinel structure. In normal-spinel structure, two B ions occupy two of the octahedral sites and one A occupies one of the tetrahedral sites. In an inverse-spinel structure, one of the two B ions occupies a tetrahedral site. The other B ion and the one A ion occupy octahedral sites.
8.4 What percentage of available tetrahedral sites is occupied by either $\mathrm{Fe}^{2+}$ or $\mathrm{Fe}^{3+}$ ion in $\mathrm{Fe}_{3} \mathrm{O}_{4}$ ?
8.5 $\mathrm{Fe}_{3} \mathrm{O}_{4}$ has an inverse-spinel structure. Draw the crystal field splitting pattern of $\mathrm{Fe}^{2+}$ and fill out the electrons. The electron pairing energy is greater than the octahedral field splitting.

## SOLUTION

8.1 (1): C
(2): $C$
(3): CO
8.2 Balanced equation (3): $\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})+3 \mathrm{CO}(\mathrm{g}) \rightarrow 2 \mathrm{Fe}(\mathrm{s})+3 \mathrm{CO}_{2}(\mathrm{~g})$
(1)

$$
\mathrm{C}(\mathrm{~s})+\mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{CO}_{2}(\mathrm{~g}) \quad \Delta H_{(1)}^{0}=-393.51 \mathrm{~kJ}=\Delta H_{f}^{0}\left(\mathrm{CO}_{2}(\mathrm{~g})\right)
$$

(2) $\quad \mathrm{CO}_{2}(\mathrm{~g})+\mathrm{C}(\mathrm{s}) \rightarrow 2 \mathrm{CO}(\mathrm{g}) \quad \Delta H^{0}(2)=172.46 \mathrm{~kJ}$

From (1) and (2):
$\Delta H_{f}^{0}(\mathrm{CO}(\mathrm{g}))=(1 / 2)\{172.46+(-393.51)\}=-110.525 \mathrm{~kJ}$

$$
\begin{aligned}
& \Delta H_{f}^{0}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)=-824.2 \mathrm{~kJ} \\
& \begin{aligned}
\Delta H_{(3)}^{0} & =3 \times \Delta H_{f}^{0}\left(\mathrm{CO}_{2}(\mathrm{~g})\right)-\Delta H_{f}^{0}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}\right)-3 \times \Delta H_{f}^{0}(\mathrm{CO}(\mathrm{~g})) \\
\quad & =[3 \times(-393.51)]-(-824.2)-[3 \times(-110.525)]=-24.8 \mathrm{~kJ} \\
\Delta S_{(3)}^{0} & =(2 \times 27.28)+(3 \times 213.74)-87.4-(3 \times 197.674)=15.36 \mathrm{~J} \mathrm{~K}^{-1}
\end{aligned} \\
& \begin{aligned}
\Delta G_{(3)}^{0} & =\Delta H^{0}-T \Delta S^{0}=-24.8 \mathrm{~kJ}-\left(15.36 \mathrm{~J} \mathrm{~K}^{-1} \times 1 \mathrm{~kJ} / 1000 \mathrm{~J} \times 1473.15 \mathrm{~K}\right)= \\
\quad= & -47.43 \mathrm{~kJ} \\
K= & \mathrm{e}^{\left(-\Delta G^{\circ} / R T\right)}=\mathrm{e}^{\left(47430 \mathrm{~J} /\left(8.314 \mathrm{~J} \mathrm{~K}^{-1} \times 1473.15 \mathrm{~K}\right)\right)}=48
\end{aligned}
\end{aligned}
$$

8.3 One $\mathrm{AB}_{2} \mathrm{O}_{4}$ unit has available $4(=1+(1 / 4 \times 12)$ octahedral sites.
8.4 Since one face-centered cube in $\mathrm{AB}_{2} \mathrm{O}_{4}$ represents one $\mathrm{Fe}_{3} \mathrm{O}_{4}$ unit in this case, it has 8 available tetrahedral sites. In one $\mathrm{Fe}_{3} \mathrm{O}_{4}$ unit, 1 tetrahedral site should be occupied by either one $\mathrm{Fe}^{2+}$ (normal-spinel) or one $\mathrm{Fe}^{3+}$ (inverse-spinel). Therefore, in both cases, the calculation gives $(1 / 8) \times 100 \%=12.5 \%$ occupancy in available tetrahedral sites.

## 8.5



## PROBLEM 9

## Photolithographic process

Photolithography is a process used in semiconductor device fabrication to transfer a pattern from a photomask to the surface of a substrate. In a typical photolithography process, light is projected, through a mask that defines a particular circuitry, onto a silicon wafer coated with a thin layer of photoresist.

The earliest photoresists were based on the photochemistry that generates a reactive intermediates from bis(aryl azide). Patterning becomes possible through the cross-linking reaction of the nitrenes generated from the azides.

9.1 Draw two possible Lewis structures of $\mathrm{CH}_{3}-\mathrm{N}_{3}$, the simplest compound having the same active functional group of bis(aryl azide). Assign formal charges.
9.2 Draw the Lewis structure of nitrene expected from $\mathrm{CH}_{3}-\mathrm{N}$.
9.3 Draw the structures for two possible products, when this nitrene from $\mathrm{CH}_{3}-\mathrm{N}_{3}$ reacts with ethylene gas $\left(\mathrm{CH}_{2} \mathrm{CH}_{2}\right)$.

Photoresists consisting of Novolak polymers, utilizes acid to change their solubility. The acid component can be produced photochemically from diazonaphthaquinone. In fact, "Novolaks" have been the representative "positive" photoresists of the modern microelectronic revolution.


Novolak

When irradiated, diazonaphthaquinone undergoes photochemical decomposition followed by rearrangement eventually producing a carboxylic acid.


Diazonahpthaquinone derivative
9.4 Draw three Lewis structures of diazoacetaldehyde (see below), the simplest compound having the same active functional group of diazonaphthaquinone. Indicate formal charges.

Diazonaphthaquinone derivative

diazoacetaldehyde
9.5 Draw a Lewis structure of the rearranged intermediate, A (see below), generated from diazoacetaldehyde after losing $\mathrm{N}_{2}$. A satisfies Lewis' octet rule and reacts with water to form acetic acid, $\mathrm{CH}_{3} \mathrm{COOH}$.


Advanced photoresists were invented in 1982 based on chemical amplification. The most popular chemical amplification for positive-tone involves the acid catalyzed deprotection of poly(p-hydroxystyrene) resin protected by various acid-sensitive protecting groups such as $t$-butyloxycarbonyl ( $t$-BOC).


The thermal decomposition of carbonate ester itself normally occurs well above $150{ }^{\circ}$ C.
9.6 Two plausible mechanisms have been suggested for this decomposition reaction having relatively high activation energy. Draw expected intermediates and products from this reaction.

9.7 In the presence of a trace amount of acid, the reaction temperature can be reduced to below $100{ }^{\circ} \mathrm{C}$. Draw expected intermediate F from the following chemical amplification process based on using $t$-BOC.


## SOLUTION

## 9.1


9.2

9.3


9.4



9.5

$$
\mathrm{O}=\mathrm{C}=\mathrm{CH}_{2}
$$

9.6


## 9.7



F

## PROBLEM 10

Natural Products - Structural Analysis


Licorice (Glycyrrhizia. Uralensis)


Licorice Root

The flavour extracted from the licorice root is $50-150$ times sweeter than table sugar. The most important and abundant compound responsible for the sweetness and medicinal effects of licorice is glycyrrhizin $\left(\mathrm{C}_{42} \mathrm{H}_{62} \mathrm{O}_{16}\right)$.

Glycyrrhizin requires three equivalents of NaOH to effect neutralization. When glycyrrhizin was subjected to acid hydrolysis, Glycyrrhizinic acid $\left(\mathbf{A}\left(\mathrm{C}_{30} \mathrm{H}_{46} \mathrm{O}_{4}\right)\right)$ and $\mathbf{B}$ $\left(\mathrm{C}_{6} \mathrm{H}_{10} \mathrm{O}_{7}\right)$ were obtainned in a 1:2 molar ratio (Scheme 1).

Scheme 1


When glycyrrhizin was methylated with methyl iodide (Mel) at every possible site before hydrolysis, hydrolysis produced $\mathbf{A}^{\prime}$ (methyl glycyrrhizinate), C and D (Scheme 2). $\mathbf{B}, \mathbf{C}$ and $\mathbf{D}$ exist as mixtures of anomers.

## Scheme 2



Methylation of $\mathbf{C}$ and $\mathbf{D}$ with Mel produced the same isomeric mixture of compounds, $\mathbf{J}$ (Scheme 3).

Scheme 3

$$
\mathbf{C}\left(\mathrm{C}_{9} \mathrm{H}_{16} \mathrm{O}_{7}\right) \stackrel{\mathrm{MeI}, \mathrm{Ag}_{2} \mathrm{O}}{\longrightarrow} \mathbf{J}\left(\mathrm{C}_{11} \mathrm{H}_{20} \mathrm{O}_{7}\right) \stackrel{\mathrm{MeI}, \mathrm{Ag}_{2} \mathrm{O}}{\rightleftarrows} \mathbf{D}\left(\mathrm{C}_{10} \mathrm{H}_{18} \mathrm{O}_{7}\right)
$$

C was reduced with $\mathrm{LiAlH}_{4}$ to give $\mathbf{K}$, and $\mathbf{L}$ was produced by the reduction of $\mathbf{K}$. Oxidative cleavage of vicinal diol of $\mathbf{L}$ with $\mathrm{NaIO}_{4}$ produced $\mathbf{M}$ and two equivalents of formaldehyde. Reduction of M produced $\mathbf{N}$. The structure and stereochemistry of $\mathbf{N}$ was confirmed by the synthesis of $\mathbf{N}$ from $\mathrm{D}-(-)$-tartaric acid through methylation followed by reduction (Scheme 4). A ${ }^{1} \mathrm{H}$-NMR spectrum of L showed two distinct peaks for methyl groups. (There is no symmetry in L)

Scheme 4

10.1 Complete structures for $\mathbf{L}, \mathbf{M}$, and $\mathbf{N}$ in the answer sheet.
10.2 How many structures for $\mathbf{C}$ are possible? Complete possible structures for $\mathbf{C}$.

To determine the correct structure of $\mathbf{C}$, following set of reactions were performed. $\mathbf{J}$ was reduced to $\mathbf{E}$, and acid hydrolysis of $\mathbf{E}$ produced $\mathbf{F}$. Reduction of $\mathbf{F}$ generated $\mathbf{G}$, and $\mathbf{G}$ was oxidized with $\mathrm{NaIO}_{4}$ to $\mathbf{H}$ with formation of one equivalent of formaldehyde. I was obtained from $\mathbf{H}$ through reduction. Among all compounds from A to I, only I was optically inactive (Scheme 5).

Scheme 5

10.3 Complete structures for $\mathbf{G}$ and $\mathbf{I}$.
10.4 Which one is the correct structure for C among ones you have drawn in 10-2?
10.5 Complete structures for B, D, and J.
10.6 Complete the structure for Glycyrrhizin.

## SOLUTION

10.1

10.2 Number of possible structures

1

10.3

G

10.4

The correct structure for $\mathbf{C}$ from $10-2$ is No. 1
10.5



J

10.6


## PROBLEM 11

## Enzyme Reaction

Shikimic acid biosynthesis is an important pathway for amino acids, alkaloids and heterocyclic natural product production. Nature converts shikimic acid to chorismic acid through a cascade of enzymatic reactions. Then chorismate mutase catalyzes the conversion of chorismic acid to prephenic acid at the branch point for the biosynthesis of aromatic amino acids such as tyrosine and phenylalanine.

11.1 During the transformation of shikimic acid to chorismic acid, dehydration is occurring. Choose the hydroxyl group in shikimic acid that is lost through above dehydration among all possible reactions.
11.2 Chorismate mutase rearranges chorismic acid into prephenic acid without changing the molecular formula. Chorismic acid becomes prephenic acid through the Claisen rearrangement, a concerted pericyclic process like the Cope rearrangement as shown below:


Based on the following spectral data, propose the structure of prephenic acid.
${ }^{1} \mathrm{H}-\mathrm{NMR}\left(\mathrm{D}_{2} \mathrm{O}, 250 \mathrm{MHz}\right): \delta 6.01(2 \mathrm{H}, \mathrm{d}, \mathrm{J}=10.4 \mathrm{~Hz}), 5.92(2 \mathrm{H}, \mathrm{dd} \mathrm{J}=10.4,3.1 \mathrm{~Hz}), 4.50$ $(1 \mathrm{H}, \mathrm{t}, \mathrm{J}=3.1 \mathrm{~Hz}), 3.12(2 \mathrm{H}, \mathrm{s})$. Note that there are three protons, which have been exchanged by $\mathrm{D}_{2} \mathrm{O}$ very fast, and two protons at $\delta 3.12$, which are exchanged slowly in prephenic acid. ${ }^{13} \mathrm{C}-\mathrm{NMR}\left(\mathrm{D}_{2} \mathrm{O}, 75 \mathrm{MHz}\right): \delta 203,178,173,132$ (for two identical carbons), 127 (for two identical carbons), 65, 49, 48.
$\delta$, chemical shift; H, integrals; d, doublet; dd, doublet of doublet; J, coupling constant; t , triplet; s, singlet


Chorismate mutase is believed to stabilize the transition state of Claisen rearrangement. Thus it is an interesting target for inhibitor design. Inhibitors, called transition state analog (TSA)s that resemble the transition state (TS, e.g., the species in brackets "[ ]" above) of the reaction are designed to occupy the active site. Several inhibitors were designed and synthesized, and among them eight turned out to be potent inhibitors of the enzyme. The lower is the $\mathrm{IC}_{50}$ (inhibitor concentration of $50 \%$ of the enzymatic activity) value, the better is the inhibitor.


1
$\mathrm{IC}_{50}=2.5 \mathrm{mM}$


2
$\mathrm{IC}_{\mathbf{5 0}}=\mathbf{1 . 3} \mathbf{~ m M}$


6
$\mathrm{IC}_{50}=0.017 \mathrm{mM}$


3
$\mathbf{I C}_{\mathbf{5 0}}=\mathbf{0 . 7 8} \mathbf{~ m M}$


7
$\mathrm{IC}_{50}=\mathbf{0 . 0 0 5 9} \mathbf{~ m M}$


4
$\mathrm{IC}_{50}=1.1 \mathrm{mM} \quad \mathrm{IC}_{\mathbf{5 0}}=\mathbf{5 . 3} \mathbf{~ m M}$


8
$\mathrm{IC}_{50}=\mathbf{0 . 0 0 0 1 5} \mathbf{~ m M}$
11.3 Choose all correct statements based on the structures and $\mathrm{IC}_{50}$ values of above inhibitors. Increase of factor 5 is considered to be important.
(a) Configuration of the hydroxyl group plays an important role in the TS and inhibitor design.
(b) The presence of both carboxylic groups is important in the TS and inhibitor design.
(c) Transition state of the reaction contains two six-membered rings with one chair and one twist-boat conformation.
(d) 7 and 8 can be distinguished on the basis of the ${ }^{1} \mathrm{H}-\mathrm{NMR}$ of $\mathrm{H}_{\mathrm{a}}$.
11.4 Draw the transition state of the transformation of chorismic acid to prephenic acid based on the TSA structures and their $\mathrm{IC}_{50}$ values.
11.5 Compared with the uncatalyzed thermal conversion, chorismate mutase accelerates conversion of chorismic acid to prephenic acid $1.0 \times 10^{6}$ fold at $25^{\circ} \mathrm{C}$ by lowering the activation energy of the reaction. Calculate the decrease in activation energy of chorismate mutase at $25^{\circ} \mathrm{C}$.
$\Delta H^{\neq}$uncat is $86,900 \mathrm{~J} \mathrm{~mol}^{-1}$ for the thermal conversion of chorismic acid to prephenic acid. At what temperature will the rate of the uncatalyzed thermal conversion be the same as that of the enzyme-catalyzed conversion at $25^{\circ} \mathrm{C}$, assuming that $E_{a}=\Delta H^{\neq}$.

## SOLUTION

11.1 Hydroxyl group No. 3
11.2

11.3 Correct statements: (a), (c), (d).
11.4


Transition state
11.5 For the enzyme-catalyzed reaction, Arrhenius equation could be applied.

$$
\begin{aligned}
& \frac{k_{\text {cat }}}{k_{\text {uncat }}}=\frac{A \exp \left(-E_{a, \text { cat }} / R T\right)}{A \exp \left(-E_{a, \text { uncat }} / R T\right)}=\exp \left[-\Delta E_{a, \text { cat-uncat }} / R T\right]= \\
& =\frac{\exp \left(-\Delta E_{a, \text { cat-uncat }}\left(\mathrm{J} \mathrm{~mol}^{-1}\right)\right.}{2,480 \mathrm{~J} \mathrm{~mol}^{-1}}=1 \times 10^{6}
\end{aligned}
$$

Therefore, $-\Delta E_{a \text {, cat-uncat }}=34,300 \mathrm{~J} \mathrm{~mol}^{-1}$
$\frac{k_{\text {uncat }, T}}{k_{\text {uncat, } 298}}=\frac{A \exp \left(-\Delta H^{\neq}{ }_{\text {uncat }} / R T\right)}{A \exp \left(-\Delta H_{\text {uncat }}^{\neq} / 298 R\right)}=\exp \left[\left(\frac{-\Delta H^{\neq}{ }_{\text {uncat }}}{R}\right)\left(\frac{1}{T}-\frac{1}{298}\right)\right]$
$\frac{k_{\text {uncat }, T}}{k_{\text {uncat, } 298}}=13.8=\exp \left[\left(\frac{-86900}{8.32}\right)\left(\frac{1}{T}-\frac{1}{298}\right)\right]$
Therefore, $T=491 \mathrm{~K}$, or $218{ }^{\circ} \mathrm{C}$

## PRACTICAL PROBLEMS

## PROBLEM 1 (Practical)

## Reverse-phase Chromatography: Spectrophotometric Analysis

Chromatographic separation followed by spectrophotometric analysis is one of the most widely practiced analytical techniques in chemical laboratories around the world. For example, organic compounds in a complex mixture are often analyzed by reverse-phase liquid chromatography with spectrophotometric detection. In reverse-phase chromatography, hydrophobic interactions between the stationary phase material (usually octadecyl group) and the non-polar moiety of the analyte is utilized. The chromatogram can be simplified and the compound of interest selectively determined by proper choice of the detector wavelength. In this part of the Practical Test, spectrophotometric analysis of dyes, with and without separation, will be performed.

1.1 Spectrophotometric Analysis of $R$ and $B$ in a Mixed Solution
a) Measure absorbance of both Solutions $R\left(3.02 \times 10^{-5} \mathrm{M}\right)$ and $B\left(1.25 \times 10^{-5} \mathrm{M}\right)$ (Fig. A \& B). Fill in the Table in the Answer Sheet with your measurements. Draw absorption spectra for the red dye in red ink and for the blue dye in blue ink (Fig. 1.1).
b) Repeat absorbance measurements for Solution MD. Solution MD is a mixture of Solution $R$ and $B$ in a certain ratio. Add the spectrum in black ink to Fig. 1.1.
c) Based on the Beer-Lambert law, determine the molar concentration of both dyes in Solution MD using the data in the Table. Do not determine the fraction of one dye by subtracting the fraction of another dye from 1.
1.2 Chromatographic Separation Followed by Spectrophotometric Analysis
a) Elute the cartridge with about $10 \mathrm{~cm}^{3}$ of Solution E using $10 \mathrm{~cm}^{3}$ syringe (Fig. C).
b) Load $1.00 \mathrm{~cm}^{3}$ of solution MD onto the cartridge (Fig. D).
c) Using $1 \mathrm{~cm}^{3}$ syringe, elute with Solution E (Fig. E). Collect the solution eluting through the outlet in a $10 \mathrm{~cm}^{3}$ volumetric flask. Repeat until the red compound is completely eluted and collected.
d) Fill the flask to the $10 \mathrm{~cm}^{3}$ mark with Solution E and mix. Call this Solution F.
e) Obtain the absorption spectrum of solution F as in Experiment 1.1. Dilution takes place during elution. Therefore, multiply the measured absorbance by 10 when drawing the spectrum for Solution F. Draw spectrum with broken line in Fig. 1.1 in red ink.
f) Dilute Solution $R$ as necessary and construct a calibration curve, at a wavelength of your choice, for analysis of the red dye (R) in Solution F. Draw a calibration curve in the answer sheet (X-axis, concentration; Y-axis, absorbance, Fig. 1.2). Indicate the wavelength used. The calibration curve must have three points in addition to the origin. Mark the position of Solution F on the calibration curve.
g) Report the concentration of $R$ in the original Solution MD.
h) Compare this concentration with the value you obtained in Experiment 1-1 and report the recovery (amount eluted/amount loaded) associated with chromatography.

## PROBLEM 2 (Practical)

## Reverse-phase Chromatography:

## Acid-Base Titration of Acetic Acid and Salicylic Acid

Acetic acid (AA) and salicylic acid (SA) are slightly different in polarity and thus can be separated on a reverse-phase cartridge using distilled water as eluent. AA is eluted first. The total amount of $A A$ and $S A$ in a mixed solution will be determined by titration. Then, AA and SA will be separately determined following chromatographic separation.

2-1. Determination of the Total Amount of AA and SA in a Mixed Acid (MA) Solution
a) Titrate $10 \mathrm{~cm}^{3}$ of distilled water with the $\mathrm{NaOH}(<5 \mathrm{mM})$ solution provided. Report blank acidity in $1 \mathrm{~cm}^{3}$ of distilled water in terms of the volume of the NaOH solution. Take this blank acidity into account for all solutions in subsequent data analyses. Show corrections in the calculation part in the answer sheet.
b) Standardize NaOH solution with $2.00 \mathrm{~cm}^{3}$ of the standard KHP (potassium hydrogen phthalate) solution $\left(1.00 \times 10^{-2} \mathrm{M}\right)$ provided. Repeat and report the concentration of the NaOH solution. Show how you accounted for the blank acidity.
c) Withdraw $1.00 \mathrm{~cm}^{3}$ of Solution MA and determine the total acidity. Repeat and report the total number of moles of $A A$ and $S A$ combined in $1.00 \mathrm{~cm}^{3}$ of Solution MA.

2-2. Reverse-phase Separation and Titration
a) Elute a new $\mathrm{C}-18$ cartridge with about $10 \mathrm{~cm}^{3}$ of distilled water using $10 \mathrm{~cm}^{3}$ syringe.
b) Load $1.00 \mathrm{~cm}^{3}$ of Solution MA onto the cartridge. Collect the liquid eluting at the outlet in tube 1 (Fraction 1).
c) Elute with $1 \mathrm{~cm}^{3}$ of distilled water. Collect the eluent in a test tube (Fraction 2). Repeat until Fraction 20 is collected. You will have 20 test tubes with about 1 $\mathrm{cm}^{3}$ liquid in each tube.
d) Titrate acidity in each test tube. Report volume of the NaOH solution consumed and the amount of acid(s) in each test tube. Make a graph in the answer sheet (Fig. 2-2) showing the amount of acid(s) in each test tube.
e) Blank acidity and the background (due to leaching out of residual materials from the column) must be subtracted. In determining the amount of eluted AA, disregard tubes containing only trace amounts of acids. Tube 2 and 3 contain most AA. Calculate the total amount of AA eluted by adding the amount of AA in tubes. Similarly calculate the total amount of SA eluted. Indicate, in Fig. 2-2, which fractions you used to get the amount of each acid.
f) Calculate the mole percent of $A A$ in solution MA.

## PROBLEM 3 (Practical)

Qualitative Analysis of Organic Compounds
In this experiment your task is to identify seven solid unknowns from the list of compounds on page 7 that are common drugs in everyday life and valuable agents in organic chemistry. To achieve this, perform chemical tests on unknowns according to the following procedures and analyze your results.

## Procedure

## Helpful Comments

a) The weight of a spatula tip-full of a solid is about $15 \sim 20 \mathrm{mg}$.
b) Wipe spatula cleanly with Kimwipe between uses.
c) After adding any reagent described below to a solution of an unknown sample, mix the contents thoroughly and observe the resulting mixture carefully.
d) To get full marks, you should perform all the tests and fill out the table.

Test 1: Solubility test
To a test tube, add a spatula tip-full (15~20 mg) of an unknown sample and $1 \mathrm{~cm}^{3}$ of $\mathrm{CH}_{3} \mathrm{CN}$. Shake the test tube and report the solubility. Repeat the test with 1 M HCl , water, and 1 M NaOH .

## Test 2: 2,4-DNPH test

Place about $15 \sim 20 \mathrm{mg}$ of an unknown sample in a test tube and dissolve with $2 \mathrm{~cm}^{3}$ of $95 \% \mathrm{EtOH}$. (For the water soluble unknowns, dissolve about 15~20 mg of an unknown in $1 \mathrm{~cm}^{3}$ of water.) Add five drops of the 2,4-dinitrophenylhydrazine solution in concentrated sulphuric acid and 95\% ethanol (labelled as 2,4-DNPH).

## Test 3: CAN test

Mix $3 \mathrm{~cm}^{3}$ of the cerium(IV) ammonium nitrate solution in dilute $\mathrm{HNO}_{3}$ (labelled as CAN) with $3 \mathrm{~cm}^{3}$ of $\mathrm{CH}_{3} \mathrm{CN}$ in a test tube. In another test tube add about $15 \sim 20 \mathrm{mg}$ of an unknown sample in $1 \mathrm{~cm}^{3}$ of the mixed solution. (For the water soluble unknown samples, dissolve about $15 \sim 20 \mathrm{mg}$ of an unknown sample in $1 \mathrm{~cm}^{3}$ of water first, and then add 1 $\mathrm{cm}^{3}$ of CAN.) If there is a colour change in the solution, the solution may contain alcohol, phenol or aldehyde.

## Test 4: Bayer test

In a test tube, dissolve about 15~20 mg of an unknown sample in $2 \mathrm{~cm}^{3}$ of $\mathrm{CH}_{3} \mathrm{CN}$. (For the water soluble unknown samples, dissolve about $15 \sim 20 \mathrm{mg}$ of an unknown in $1 \mathrm{~cm}^{3}$ of water.) To the solution, slowly add five drops of the $0.5 \% \mathrm{KMnO}_{4}$ solution, drop by drop while shaking.

## Test 5: pH test

In a test tube, dissolve about 15~20 mg of an unknown sample in $2 \mathrm{~cm}^{3}$ of $95 \% \mathrm{EtOH}$. (For the water soluble unknown samples, dissolve about 15~20 mg of an unknown sample in $1 \mathrm{~cm}^{3}$ of water). Measure the pH of the solution with pH paper.

Test 6: Iron(III) chloride test
Take the solution from Test 5 and add five drops of a $2.5 \% \mathrm{FeCl}_{3}$ solution.

## Results

1. Record your test results in the answer sheet. Write $O$ if soluble and $X$ if insoluble for the solubility tests. Write (+) for the positive reactions and ( - ) for the negative reactions for tests $2 \sim 4$ and 6 . Write $a, b$ and $n$ for acidic, basic or neutral, respectively, for pH test 5 .
2. Based on your test results, identify the most plausible structures for the unknown compounds from the provided list of compounds. Write the compound initial in appropriate box.

## Possible Unknown Compounds (next page):


(A)

(E)

(F)

(G)

(K)

(M)

(Q)

(T)

(V)

(W)

